

Spatial prediction of topsoil salinity in the Chelif Valley, Algeria, using local ordinary kriging with local variograms versus whole-area variogram

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Abstract

A novel form of ordinary kriging, involving the local estimation and modelling of the variogram at each prediction site (OKLV), is tested at a regional scale on a large data set, in order to adapt to non-uniform spatial structures and improve the assessment of the salinity hazard in the lower Chelif Valley, Algeria. The spatial variability study was carried out on a 38000 ha area using 5141 topsoil electrical conductivity (EC) measurements systematically sampled on a 250 m by 250 m grid. Variography analysis confirmed the existence of large trends in the EC variability with differing spatial structures between sub-areas.

OKLV performed better than ordinary kriging with a whole-area variogram (OKWV) in predicting the proportion of high saline soils in large blocks, but the predictions appeared mostly similar. In contrast, the estimation variance maps revealing the uncertainties of the spatial predictions were markedly different between the 2 methods. OKLV integrates the local spatial structure in the uncertainty assessment, whereas kriging with a whole-area variogram only considers the sampling intensity. Comparison with prediction errors on a validation set confirmed the consistency of the OKLV prediction variance. This appears to be a major improvement for decision-making procedures such as delineating areas where remediation should take place.

Additional keywords: soil salinity, spatial analysis, semivariogram.

Introduction

The widespread and growing phenomenon of salinisation in Mediterranean areas is related largely to climatic factors and irrigation development (Isbell *et al.* 1983; Puigdefabregas and Mendizabal 1998). The problem is acute in Algeria even in the highest productive areas like the Chelif Valley (Boulaine 1957; Daoud 1983; Saidi *et al.* 1999), but no detailed spatial analysis of its extension had been undertaken.

Geostatistics has been widely applied on electrical conductivity (EC) measurements for evaluating the salinity hazard (Hajrasuliha *et al.* 1980; Samra *et al.* 1988; Oliver and Webster 1990; Hosseini *et al.* 1994; Sylla *et al.* 1995; Odeh *et al.* 1998; Utset *et al.* 1998). An overview of modern geostatistics applied to soil survey has even been exemplified on a salinity data set (Bourgault *et al.* 1997). Nevertheless, few studies have addressed the regional variability of soil salinity. At that areal extent, spatial trends and non-stationarity of the process may affect the accuracy of classical geostatistical approaches. In addition, variations in the spatial covariance structure should be detected as they may reveal changing factors influencing salinity spatial variability.

The present work explores the application of a particular form of kriging, namely ordinary kriging with local variogram (OKLV), to assess the topsoil EC over the Chelif Valley in Algeria. In this approach, the kriging procedure is fully dependent on the local spatial structure of the salinity process and should be able to adapt to trends in the data. The aims are therefore: (1) to map the topsoil salinity in the lower Chelif Valley, an extensively irrigated area in northern Algeria; (2) to evaluate the use of local ordinary kriging with local versus whole-area variograms, where the data set consists of intensively sampled observations.

Methods

The study area

The Chelif Valley forms a 5000 km² plain (0°60 E, 36°00 N) extending eastward in the northern part of Algeria along the Chlef River (Fig. 1). Tertiary marl and limestone foothills bound the valley in the northern and southern parts. The study area is located in the lower part of the valley and covers 38000 ha with mainly irrigated fields used for growing cereals, fruits, and vegetables.

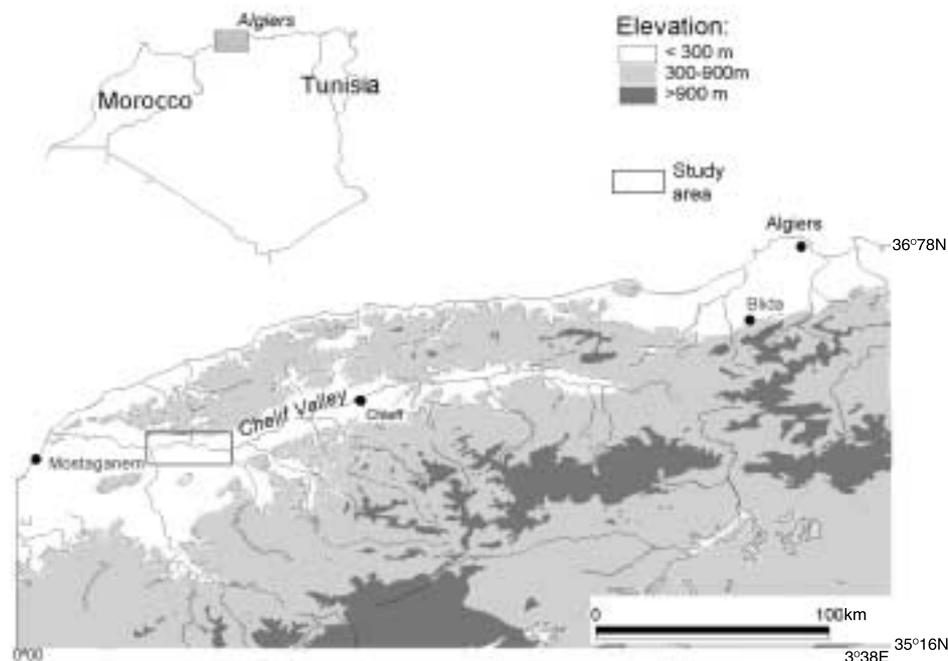


Fig. 1. Location of the study area in the Chelif Valley, Algeria.

The soils of the Chelif Valley are developed from Quaternary colluvial or alluvial material. Boulaïne (1956, 1957) identified mainly soils with weak pedological organisation: the main differentiation criteria were the texture ranging from loam to light clay, the calcareous content, and the occurrence of vertic features. He was the first to notice a much larger proportion of saline soils in the lower part of the valley, later confirmed by Daoud (1983) and Saidi *et al.* (1999).

The lower Chelif Valley falls within the semi-arid climatic zone with an average rainfall of 370 mm in the H'madena area; this rainfall is winter dominant and occurs mainly in the form of heavy showers which may cause flooding in the lower parts of the valley. From May to September, the monthly rainfall is usually <20 mm with average temperatures above 25°C. During 1997, the year when sampling was conducted, the annual rainfall was 392 mm over 78 raindays, but of that 205 mm fell in only 5 days.

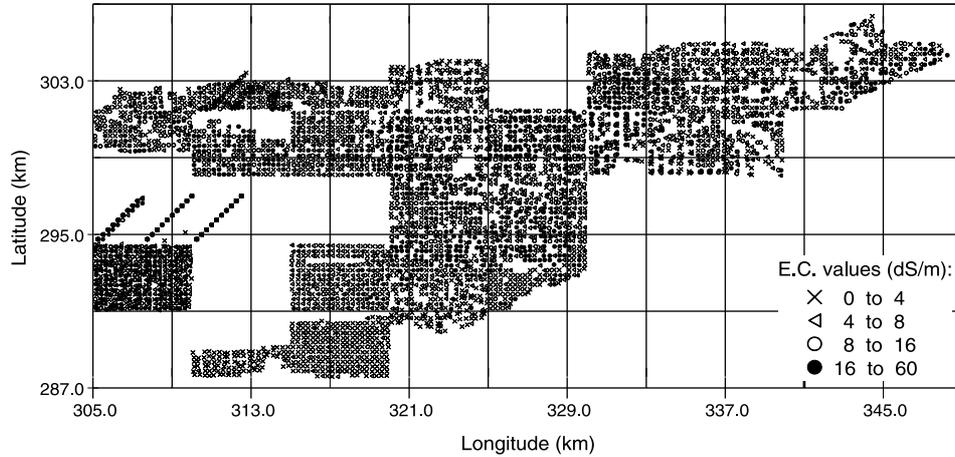


Fig. 2. Location map of the topsoil electrical conductivity data within the lower Chelif Valley. The grid lines define blocks of 16 km² used in the validation process.

The sampling process

The data set consists of 5141 sampling sites, arranged on a systematic square grid with 250-m spacing between sites (Fig. 2): thirty 1:5000 topographic maps were considered and the soil was sampled on their grid node locations where agricultural fields were present. Supplementary transects were also supplied for more detailed sampling in the western part of the area. The sampling took place during the dry season of May to September 1997.

At each site the soil was sampled at the depth of 0.0–0.20 m, air-dried, and ground to pass through a 2-mm sieve. A saturated paste of the sample was then prepared and the EC of the solution suction extract was measured and adjusted to 25°C (US Salinity Laboratory Staff 1954; Rhoades 1993).

Spatial prediction: kriging with local v. whole-area variograms

Two ordinary kriging methods (Cressie 1991) were used to predict the topsoil electrical conductivity, EC*, at any unknown location, \mathbf{x}_0 , using the measured values EC(\mathbf{x}_i) from n sampled locations \mathbf{x}_i . Both methods assume that:

$$EC^*(\mathbf{x}_0) = \sum_{i=1}^n \lambda_i EC(\mathbf{x}_i), \quad \sum_{i=1}^n \lambda_i = 1 \quad (1)$$

These 2 methods differ in the variogram estimation and modelling procedures, i.e. the way the weights λ_i in Eqn 1 are computed.

Local ordinary kriging with a whole-area variogram (OKWV)

In this conventional approach, a unique semivariogram is inferred and modelled for the whole data set, providing a global spatial covariance structure over the whole study area. Assuming local stationarity of the mean, the kriging prediction is limited to observations in the neighbourhood of any unknown point and their weights are obtained by minimising the prediction error under a non-bias condition (Cressie 1991). The prediction variance $\sigma^2(\mathbf{x}_0)$, i.e. the minimised mean-square error, is also estimated at each unknown location through:

$$\sigma^2(\mathbf{x}_0) = \psi + \sum_{i=1}^n \lambda_i \gamma(\mathbf{x}_i, \mathbf{x}_0) \quad (2)$$

Where ψ is a Lagrange multiplier and $\gamma()$ is the semivariogram model.

OKWV was performed to predict EC* at points or over 100 m by 100 m blocks by fitting a double exponential function to the mean experimental variogram (Fig. 3) and adopting a neighbourhood of 100 observations around each prediction site.

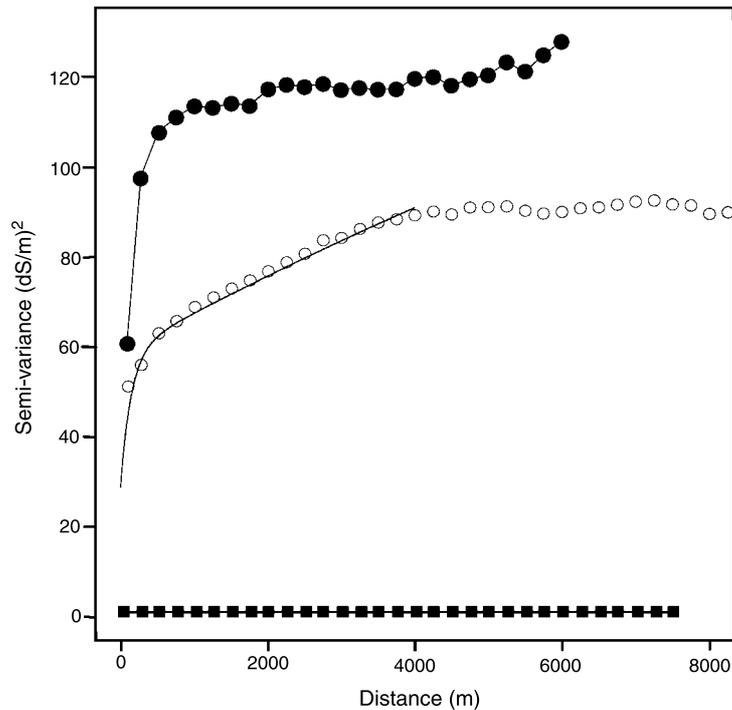


Fig. 3. Electrical conductivity mean experimental variograms over the whole area (○) and for two sub-areas: (■) the area south of 291 km; (●) the rectangular area with opposite corner co-ordinates [320 293] and [330 301]. A double-exponential model is fitted on the whole-area variogram.

Ordinary kriging with a local variogram (OKLV)

Unlike the previous approach, OKLV involves the estimation and modelling of the variogram in the neighbourhood of each unknown site \mathbf{x}_0 . A local spatial covariance model is therefore established around each point and used in Eqns 1 and 2 to estimate the property and its estimation variance.

This method was initially developed by Haas (1990a, 1990b) as a tool to map properties affected by spatial trend or changing covariance structure and applied to estimate rainfall sulfate deposition at a continental scale with a relatively sparse sample (160 monitoring sites). Further development considered the combined spatial and temporal variability of similar property (Haas 1995). On a quite finer resolution, namely an individual farm field, prediction with local variogram was also found to be well-suited to mapping crop yields using intensively measured data (with thousands of sites) obtained by continuous yield monitoring (McBratney *et al.* 1996; Whelan 1998). The ability of the method to adapt to situations of marked differences in local structure from the overall spatial variability was quoted as its main interest and explains its growing application in precision agriculture.

OKLV was applied to predict the EC at points or over 100 m by 100 m blocks. For each unknown site, the experimental variogram was computed considering a neighbourhood of 100 observations within a mean radius of 1650 m varying with the sampling density. This procedure was chosen to estimate the variogram with at least 100 sampling points as suggested by Webster and Oliver (1990). Haas (1995) proposed to use cross-validation to find the minimum size of the local data set, but this method appeared too computationally expensive.

An exponential model was fitted automatically using non-linear least-squares optimisation weighted by the number of pairs in the variogram. The exponential model was chosen because of its flexibility in fitting the variogram. The computation was done by using VESPER (Minasny *et al.* 1999) developed at The University of Sydney¹.

The validation procedures

Two validation procedures were adopted to compare the kriging techniques, testing either their prediction quality at points or their ability to evaluate the proportion of high saline soils within non-overlapping blocks.

Prediction quality at points

400 points have been selected at random and considered as a validation set. The prediction quality was determined by comparing the actual EC values with EC* kriging estimates using the remaining points. Three prediction quality criteria were considered: (i) the mean error (ME), (ii) the root mean-square error (RMSE), and (iii) the mean rank of each method (MR). If m is the number of validation points:

$$\text{ME} = \frac{1}{m} \sum_{i=1}^m [\text{EC}^*(\mathbf{x}_i) - \text{EC}(\mathbf{x}_i)] \quad \text{RMSE} = \sqrt{\frac{1}{m} \sum_{i=1}^m [\text{EC}^*(\mathbf{x}_i) - \text{EC}(\mathbf{x}_i)]^2}$$

$$\text{MR}_{\text{OKWV}} = \frac{1}{m} \sum_{i=1}^m r(\mathbf{x}_i) \quad \text{where}$$

$$\begin{cases} r(\mathbf{x}_i) = 1 & \text{if } |\text{EC}^*_{\text{OKWV}}(\mathbf{x}_i) - \text{EC}(\mathbf{x}_i)| \leq |\text{EC}^*_{\text{OKLV}}(\mathbf{x}_i) - \text{EC}(\mathbf{x}_i)| \\ r(\mathbf{x}_i) = 2 & \text{otherwise} \end{cases}$$

$$\text{MR}_{\text{OKLV}} = 3 - \text{MR}_{\text{OKWV}}$$

The reliability of the prediction variances estimated by each method was also tested on the validation set by computing the mean standardised squared error (MSSE):

$$\text{MSSE} = \frac{1}{m} \sum_{i=1}^m \frac{(\text{EC}^*(\mathbf{x}_i) - \text{EC}(\mathbf{x}_i))^2}{\sigma^2(\mathbf{x}_i)}$$

MSSE should be close to 1 if the kriging variance is an accurate estimate of the actual error variance (Wackernagel 1998).

Another way to assess the prediction variance consisted of combining the prediction estimate and prediction variance to derive a Gaussian-type confidence interval centred on the prediction estimate (Cressie 1991): a 95% confidence interval of EC* was estimated at each validation site \mathbf{x}_i , by $[\text{EC}^*(\mathbf{x}_i) - 2\sigma(\mathbf{x}_i); \text{EC}^*(\mathbf{x}_i) + 2\sigma(\mathbf{x}_i)]$. Computing the proportion of validation points where the 95% confidence interval actually includes the true value tested this approach. This proportion should be near 95% for an accurate modelling of uncertainty.

Prediction quality of high saline soils proportion within blocks.

We tested also the ability of the kriging methods to evaluate the proportion of high saline soils within large blocks, with the notion of, for example, selecting for remediation the most affected ones. The study area was therefore divided into 4 km by 4 km blocks (Fig. 2) and the data set was randomly equally split into prediction and validation sites. 17 blocks mostly included in the study area were considered; in each block, the actual proportion of soils with EC values exceeding a threshold of 16 dS/m was derived from 80–120 available validation sites. OKWV and OKLV were then performed at the validation sites using the

¹Compiled program available from Australian Centre for Precision Agriculture, University of Sydney: www.usyd.edu.au/su/agric/acpa

prediction set, and their respective predicted proportion of values exceeding 16 dS/m was calculated. The prediction quality of this proportion was also determined as before through ME, RMSE, and MR criteria.

Results

Exploratory data analysis

The histogram of the 5141 EC data was highly skewed with values ranging from 0.2 to 58.7 dS/m and a median value of 5.4 dS/m (Fig. 4). Compared with the thresholds based on crop salt tolerance (US Salinity Laboratory Staff 1954), 36 % of the samples were considered non- or slightly-saline (<4 dS/m), 48 % saline ([4–16] dS/m) and 16 % highly saline (>16 dS/m).

The location map of the data (Fig. 2) revealed sharp regional trends with varying mean EC values and spatial variability; for instance, low and almost uniform values were observed in the southern part, whereas the central part exhibits higher values and short distance variability. The semivariogram of the whole area had a large nugget effect, about 50% of the total variance (Fig. 3, circles). Two spatial variation structures could be distinguished from the inflexions of the experimental curve: a local scale (range ~ 500 m) and a regional scale (range ~ 4000 m). This variogram was best fitted up to a distance of 4000 m with a double-exponential model with a nugget value of 28.8 (dS/m)², sill parameters of 29 and 153 (dS/m)², and distance parameters of 150 and 17000 m:

$$\gamma(h) = 28.8 + 29 \left[1 - \exp\left(-\frac{h}{150}\right) \right] + 153 \left[1 - \exp\left(-\frac{h}{17000}\right) \right] \text{ if } h \leq 4000$$

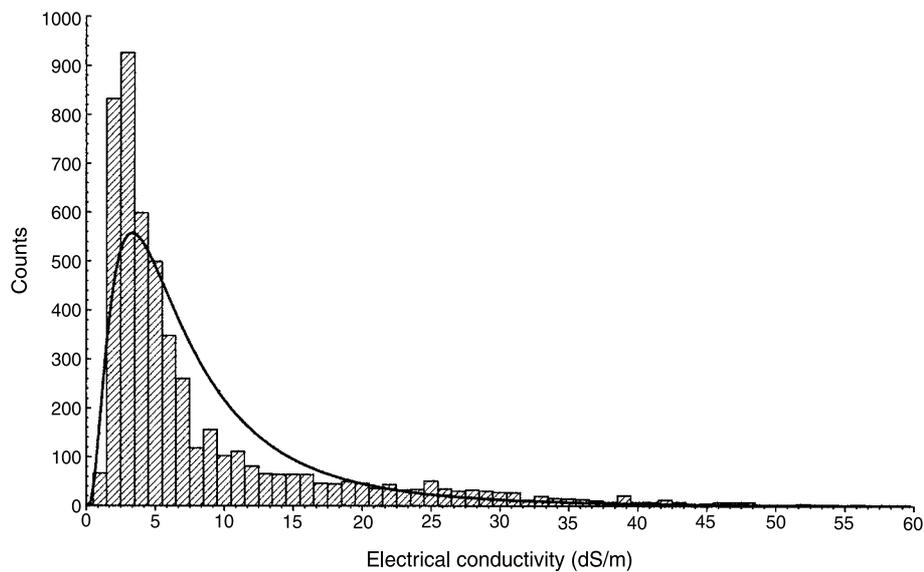


Fig. 4. Frequency distribution of the saturated soil paste electrical conductivity for the 5141 samples, with representation of a fitted lognormal distribution.

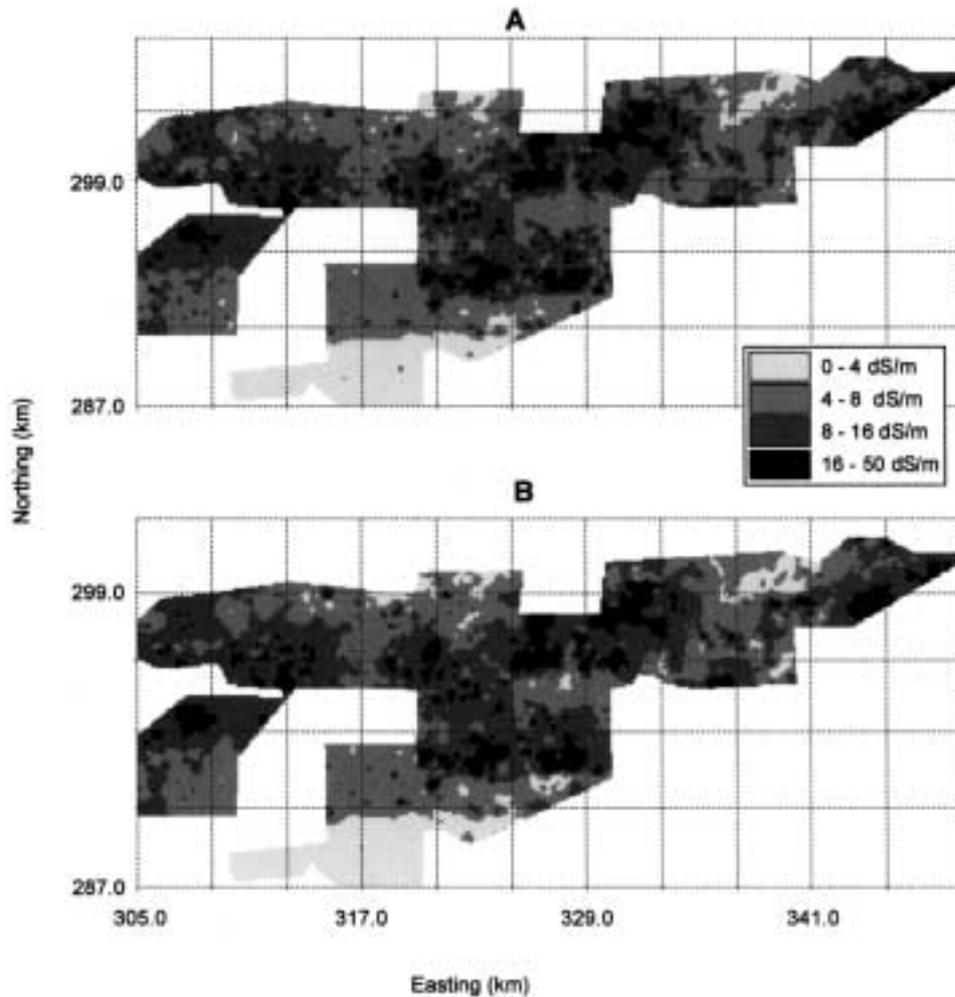


Fig. 5. Electrical conductivity maps constructed by (a) OKWV using a double exponential model; (b) OKLV using an exponential model fitted on a local variogram estimated from 100 nearest points.

Beyond 4000 m, the semi-variance appeared to be constant. When limiting the variography analysis to sub-areas, the previously observed sharp differences between sectors became apparent. The experimental variogram for the southern area indicated weak variability and lack of spatial structure (Fig. 3, squares); by contrast, the semivariogram of the central area (Fig. 3, discs) showed a huge spatial variability marked by a high nugget effect and an exponential shape increase until 1500 m. These differences between sub-areas may be related to changing topographic and lithologic conditions, but other explanation factors have also to be considered (land use, quality of irrigation water) and the spatial trends are therefore not fully understood.

Topsoil electrical conductivity prediction

The prediction maps of the electrical conductivity in the lower Chelif Valley were obtained on 37906 sites by OKWV (Fig. 5a) and OKLV (Fig. 5b) using 1-ha blocks. Both maps

revealed the same trends of salinity, marked by gradual changes from low salinity areas to hot spots of very high salinity which vary from 1 ha to 8000 ha. The variance of the electrical conductivity predictions (Table 1) for both methods was much lower than the initial data, indicating a strong smoothing effect of the kriging processes.

The similarity of the prediction maps was confirmed by the results of the validation procedures. In the first test, i.e. the comparison to 400 validation points, the prediction errors of OKLV and OKWV (Table 2) were identical and there is no preferred method. In the second test comparing their ability to estimate the proportion of high saline soils in blocks, both methods underestimated this proportion (Table 2), but as stated by its lower mean rank, the OKLV method gave better results.

Table 1. Summary statistics of the electrical conductivity for the data set and for the kriging predictions over 1-ha blocks

	Counts	EC data or predictions		Prediction variance	
		Mean (dS/m)	Variance (dS/m) ²	Mean (dS/m) ²	Variance (dS/m) ⁴
Data	5141	9.0	84.5	—	—
OKWV	37906	9.2	26.6	20.7	32.3
OKLV	37906	9.2	27.1	13.8	269.4

Table 2. Validation statistics of the prediction quality at points and the prediction of the proportion of highly saline soils within 16 km² blocks

Mean error (ME), root mean-square error (RMSE), and mean rank (MR) of the methods

	EC prediction at 400 validation points			% (EC >16 dS/m) over blocks		
	ME (dS/m)	RMSE (dS/m)	MR	ME (%)	RMSE (%)	MR
OKWV	0.3	8.3	1.51	-8	13.5	1.88
OKLV	0.3	8.3	1.49	-6	11.4	1.12

Uncertainty of the predictions

By contrast with the similarity of the prediction results, OKLV and OKWV differed sharply in describing the uncertainty associated with the predictions.

For OKWV, the statistics of the prediction variance (Table 1) were characterised by a high mean value and a low variance. The corresponding map (Fig. 6a) showed slight differences in the prediction variance over the area, which were dependent on the sampling intensity. Such a pattern was expected as OKWV assumes the same covariance model over the area and only the distances between the predicted and the observed sites may affect Eqn 2.

For OKLV, the prediction variance had a lower mean and higher variance (Table 1). The resulting map had a radically different pattern (Fig. 6b); large areas with very low prediction variance (<4 dS/m)² are represented in the southern and northern parts, denoting more precise predictions of the electrical conductivity in those areas. On the other hand, areas with high prediction variance were noted both in the cases of low sampling intensity, for instance in the western part, and of high spatial variability, i.e. in central regions.

The consistency of the prediction variance for OKLV was first tested graphically by comparing the prediction errors computed on the 400 validation points against the prediction variance. Box plot statistics of the prediction errors against prediction variance

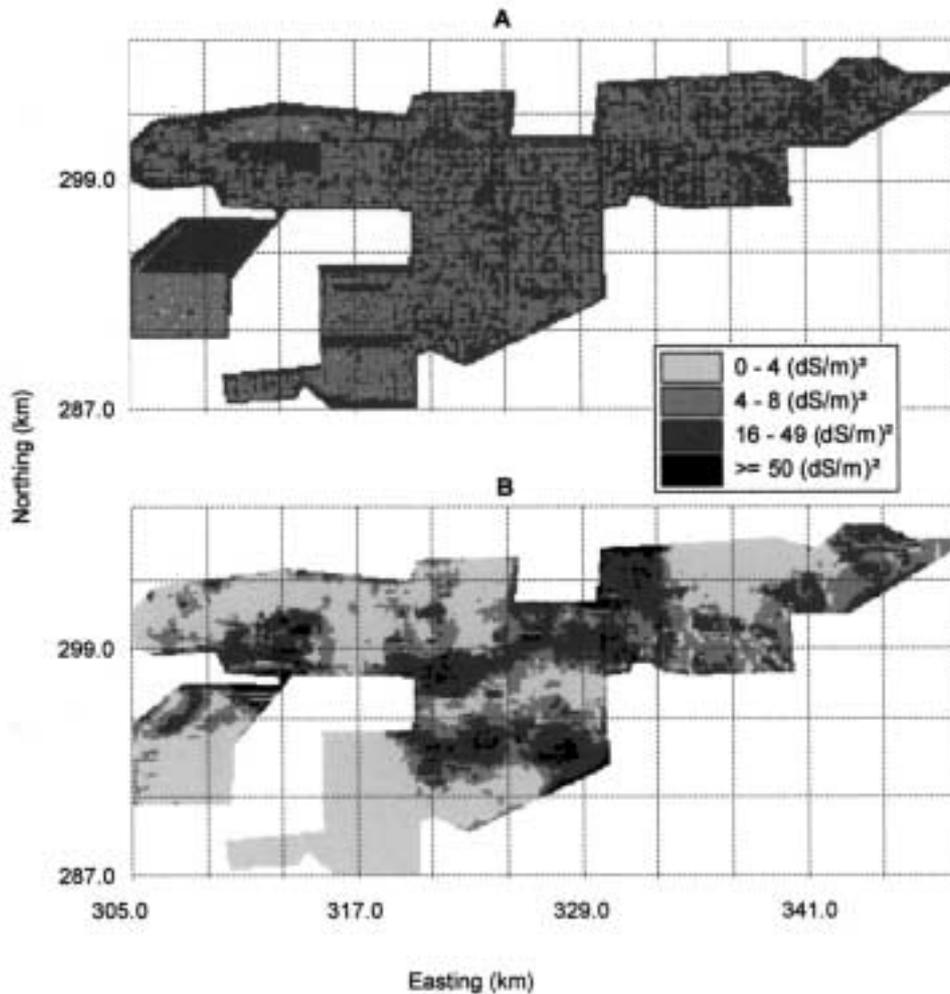


Fig. 6. Estimation variance maps of the electrical conductivity constructed by (a) OKVW using a double-exponential model; (b) OKLV using an exponential model fitted on a local variogram estimated from 100 nearest points.

classes (Fig. 7) confirmed that the prediction errors increased significantly according to the prediction variance.

Validation statistics of the prediction variance gave similar results for OKLV and OKVW (Table 3); the MSSE is about 1.1 indicating a slight underestimation of the actual prediction error by both methods, which can be attributed to the presence of a few outliers with very high values in the validation set. When considering the proportion of validation points included in the 95% confidence interval, both methods gave also similar results with 92% and 93% of the points included in that interval.

The prediction errors on the validation set therefore appeared in agreement with the prediction variances estimated by OKLV or OKVW.

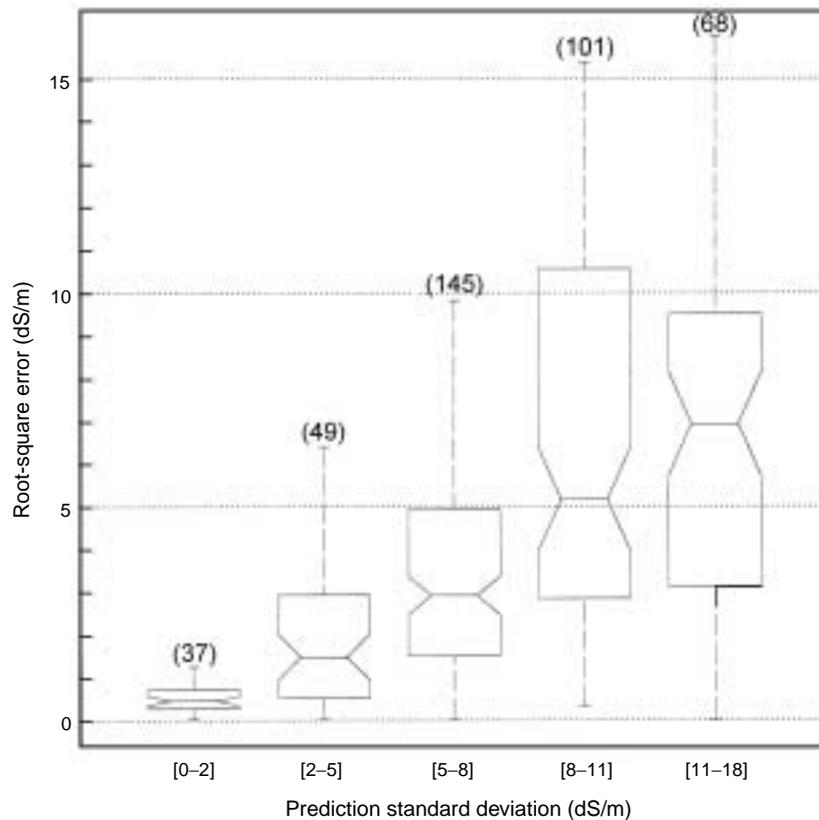


Fig. 7. Boxplot statistics for the validation set of the root-square error against 4 classes of OKLV prediction variance, with indication of the number of points within each class.

Discussion

Assessment of the topsoil salinity in the Chelif Valley

The topsoil EC in the Chelif Valley showed marked spatial structure differences between sub-areas, ranging from homogeneous low value domains to sub-areas with very high variability and superposed local and regional scales of variation. As OKLV estimates parameters of the covariance model at each prediction site, these changes can be visualised by mapping, for instance, the nugget values to assess short-range variability. Such maps may help to identify the main factors affecting salinity in each area and will be compared in an ulterior work to physiographic and irrigation practice data.

Table 3. Validation statistics of the prediction variance σ^2 at 400 points

Mean standardised squared error (MSSE) and proportion of true values included in the 95% confidence interval (P95)

	MSSE	P95 (%)
OKWV	1.17	93
OKLV	1.13	92

Estimation of areas affected by salinity in the Chelif Valley may be derived in first approximation from the ordinary kriging maps (Table 4); 43% of the valley would be considered as saline (8–16 dS/m) and 9% as highly saline (>16 dS/m). In a more rigorous approach, such an assessment must also consider the uncertainty, which may affect the salinity prediction. This may be done considering the 95% confidence interval of the electrical conductivity estimated at each unknown site \mathbf{x}_0 , by $[EC^*(\mathbf{x}_0) - 2\sigma(\mathbf{x}_0), EC^*(\mathbf{x}_0) + 2\sigma(\mathbf{x}_0)]$. An exhaustive inventory of the areas possibly affected by salinity may therefore consider the upper limit of that confidence interval, as done in Table 4 for the OKLV estimates; this leads to a sharp increase of the areas considered as highly saline, 40% of the valley being affected by salinity predictions whose confidence interval includes values above 16 dS/m.

Thus, the differences between OKLV and OKWV prediction variance estimates receive here practical signification, as shown in Fig. 8; according to OKWV, 60% of the valley has a upper confidence limit above a threshold of 16 dS/m, therefore much more than the 40% estimated by OKLV. This is to be related to the high and almost uniform OKWV prediction variance, influenced only by the sampling intensity, whereas OKLV also takes into account the local variability structure.

Table 4. Areas of topsoil EC classes according to OKLV estimates and OKLV 95% upper confidence limits

	EC class (dS/m)				Total
	[0 – 4]	[4 – 8]	[8 – 16]	>16	
	<i>EC prediction</i>				
km ²	39.99	142.82	163.36	32.89	379.06
%	10	38	43	9	100
	<i>EC upper 95% confidence limit</i>				
km ²	18.14	36.33	172.89	151.70	379.06
%	5	10	45	40	100

Kriging with local variograms

Until recently, the development of geostatistical approaches using local variograms, which could also embrace non-linear estimators such as multiple indicator kriging, was limited by computational time and scarcity of sampling data. The first limiting factor has been reduced by enhanced computing performance, and to a lesser extent, the development of comprehensive soil databases and increasing data acquisition potential reduced the sampling limitation.

Geostatistical approaches based on local variograms should therefore be reconsidered as they convey 2 types of improvements.

Detection and adaptation to spatial trends

A common situation in soil spatial analysis is where major scales of spatial variation are related to changes in land use, soil type, or lithology inducing differing spatial structures from one entity to another. Current approaches to deal with such situations include within-stratum kriging (Voltz and Webster 1990), kriging with local means (Wackernagel 1998), or kriging with an external drift (Bourenane *et al.* 1996). Where sufficient sampling intensity is available, local variograms approaches are easier to implement and less dependent on the validity of pre-existing information.

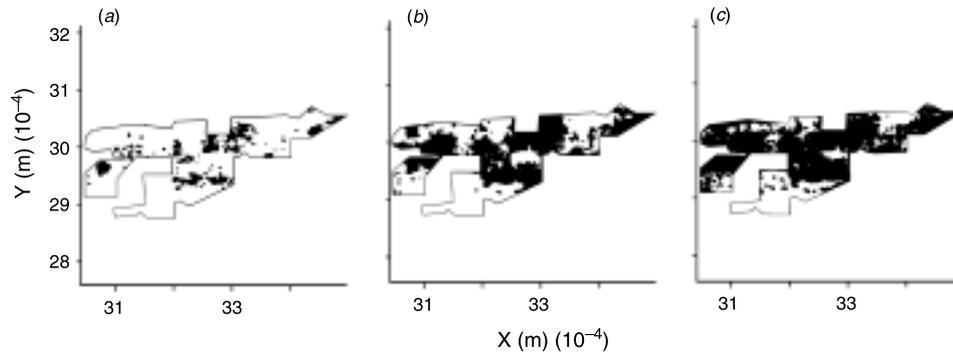


Fig. 8. Locations of EC values exceeding a threshold of 16 dS/m according to (a) OKLV estimate, (b) OKLV 95% upper confidence limit, and (c) OKWV 95% upper confidence limit.

Local uncertainty assessment

Goovaerts (1997, 1999) criticised the usual confidence interval approach for modelling local uncertainty with strong emphasis given to the inability of this approach to adapt to the local variability context. For a more straightforward assessment of the local uncertainty, he promoted therefore more complex approaches such as disjunctive kriging or non-parametric approaches. Kriging with local variograms includes the local spatial structure in the uncertainty assessment and its prediction variance appeared relevant when compared with validation points. This method improves therefore the more accessible conventional approach of uncertainty assessment in case studies where broad indicators of this uncertainty are sufficient.

An alternative approach suggested by Isaaks and Srivastava (1989) and Goovaerts (1999) could also be considered, consisting of rescaling locally the sill of the global variogram to equal the variance of the data within the kriging search neighbourhood and keeping the range constant. Indeed, OKWV and OKLV yielded similar predictions and changing the local shape of variograms had therefore little impact on prediction; hence, the local rescaling of the global semivariogram could be as good as OKLV. Nevertheless, calculating the variance within the local neighbourhood is about as computationally expensive as calculating the local variogram and therefore only limited computing speed gains should be expected.

Conclusion

The OKLV method was found to be better than OKWV to describe the topsoil salinity in the Chelif Valley through the more relevant prediction variance, which was shown to be useful in delineating areas potentially affected by high salinity. Despite enhanced computational time and the need of large data sets, geostatistical approaches of soil spatial variability based on local variograms should be developed as they convey a more informative uncertainty model of the predictions.

Finally, this study confirmed the importance of the salinity hazard in the region, with 10–40% of the areas affected. The kriging maps can serve as guide to remediation and future monitoring. In particular, in selected highly saline and variable areas, more continuous and extensive approaches of soil salinity measurement and monitoring will be developed involving remote sensing and geophysical approaches.

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Manuscript received 15 September 1999, accepted 29 June 2000